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# Quadrupolar Benzobisthiazole-Cored Arylamines as Highly Efficient Two-Photon Absorbing Fluorophores

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**S** Supporting Information

[AB](#page-3-0)STRACT: [A computer-](#page-3-0)aided design of novel  $D-\pi-A-\pi-D$ styrylamines containing five isomeric benzobisthiazole moieties as the electron-accepting core has revealed the linear centrosymmetric benzo[1,2-d:4,5-d′]bisthiazole as the most promising building block for engineering chromophores displaying high two-photon absorption (TPA) in the near-IR region, as also confirmed experimentally. The ease of synthesis of quadrupolar derivatives thereof, combined with extraordinarly high TPA action cross sections ( $\delta_{TPA}\Phi_f > 1500$ GM), makes these heteroaromatic systems particularly attractive as diagnostic agents in 3D fluorescence imaging.

[NG)  $R_2N-$ 1400  $|\mu_{01}|^2 |\mu_{12}|^2$  $1200$  $\delta_{\text{TPA}}^{\text{3SM}}$  $(E_1 - E_2/2)^2$  $\delta_{\text{TPA}}\Phi_{\text{f}}$  (810 nm)  $>1500$  GM regioisomeric effect on TPA structure-property relationships gth [nm]

Thiazole and thiazole-annulated scaffolds are among the most prominent building blocks in chromophores with potential applications in fields such as nonlinear optics  $(NLO)$ ,<sup>1−4</sup> organic light-emitting diodes,<sup>5</sup> organic field-effect transistors, $6$  and dye-sensitized solar cells.<sup>7</sup> Most of these applicat[ions](#page-3-0) rely on the electron-withdr[aw](#page-3-0)ing ability of the thiazole ri[ng](#page-3-0), which is frequently used as th[e](#page-3-0) edge substituent. Recently, we demonstrated use of the 1,3-benzothiazole moiety as an electron-accepting core in quasi-quadrupolar fluorophores with the D−π−A−π−D setup, which display high two-photon absorption  $(TPA).<sup>2</sup>$  This feature enables the activation of chemical and photophysical processes by low-energy near-IR excitation, which is [be](#page-3-0)neficial in deeper light penetration through materials or living tissues as compared to excitations by visible or UV light (lower-energy photons are also less likely to cause damage outside the focal volume). Dependency of the TPA rate on the square of the incident laser light intensity allows for better control and higher spatial resolution, which is exploited in microfabrication, high-resolution imaging and 3D data storage. To fully benefit from the advantages of the TPA process and to meet specific application requirements, a quest for dyes possessing larger TPA cross sections  $(\delta_{TPA})$  in a suitable excitation window, in conjunction with additional properties, such as high emission quantum yields, excelent photostability, and good cell permeability (keeping the molecular size as small as possible), is still a hot topic in material science.<sup>8</sup> In this respect, we were curious as to whether the introduction of a second thiazole

ring onto photochemically stable, π-deficient benzothiazole might offer a useful design strategy for enhancing TPA.

While a reasonable number of benzobisthiazole dyes has been reported to date, predominantly in the form of variously substituted 2,6-di(hetero)arylbenzo $[1,2-d:4,5-d']$ bisthiazoles,<sup>6,9</sup> TPA properties of these derivatives have remained unexplored. To the best of our knowledge, there was only one attempt [to](#page-3-0) characterize a benzobisthiazole-containing polymer (trans-PBT), which was however unsuccessful due its limited solubility.<sup>10</sup> Synthesis and spectral properties of bis(styryl)benzobisthiazole dyes, which may be viewed as analogues of the previou[sly](#page-3-0) characterized benzothiazole fluorophores and could thus allow a direct comparison of these systems, were not reported so far. Additionally, two thiazole rings could be connected to the central benzene in several different ways, resulting in five constitutional isomers (Scheme 1), namely, benzo[1,2-d:5,4-d′]bisthiazole (1), benzo[1,2-d:4,5-d′]bisthiazole (2), benzo[1,2-d:4,3-d′] bisthiazole  $(3)$ , [ben](#page-1-0)zo $[2,1-d:3,4-d']$ bisthiazole  $(4)$ , and benzo- $[1,2-d:3,4-d']$ bisthiazole  $(5)$ .

To evaluate the influence of an additional thiazole ring and the effect of positional isomerism on TPA properties, a series of linear and V-shaped quadrupolar benzobisthiazole-derived dyes, bearing N,N-dialkylaniline and triphenylamine moieties as the electron-donating groups, have been investigated in this work (Scheme 1).

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#### <span id="page-1-0"></span>Scheme 1. Structure of the Parent Benzobisthiazoles (1−5) and Quadrupolar Chromophores Q1–Q5<sup>a</sup>



<sup>a</sup>R substituents in the arylamine part are indicated by the suffix at the end of the dye label. TPA cross sections,  $\delta_{TPA}$  (S<sub>0</sub>  $\rightarrow$  S<sub>2</sub>) given in GM (1 GM =  $1 \times 10^{-50}$  cm<sup>4</sup>·s·photon<sup>-1</sup>), excitation energies  $E_{\text{n}}$ , and ground-to-excited and excited-to-excited state transition dipole moments  $\mu_{01}$  and  $\mu_{12}$ , respectively, were computed at the CAM-B3LYP/6-311++G\*\* level using a PCM solvation model (toluene as the solvent).

A computer-aided prescreening of chromophores with the highest TPA activity has been done by means of the quadratic response time-dependent DFT method, employing the CAM‑B3LYP functional and a polarizable continuum model (PCM) accounting for bulk solvent effects, as implemented in the Dalton program.  $^{11} \delta_{\rm TPA}$  associated with the five lowest excitations are collected in Supporting Information, SI. Since we found a strong depen[den](#page-3-0)cy of the TPA cross sections on the conformation o[f the two styryl branches](#page-3-0) with respect to a heteroaromatic core (s-cis and/or s-trans arrangement), all lowenergy conformers were included in our calculations, and the results were Boltzmann-averaged.<sup>12</sup> Note that  $\delta_{TPA}$  values for different conformers of the same molecule vary, in some cases, by several hundreds of GM, underli[nin](#page-3-0)g the necessity to consider conformational flexibility in rational design of TPA-active materials.<sup>13</sup>

In all cases, the highest  $\delta_{\text{TPA}}$  with maxima positioned in the red and near-[IR](#page-3-0) region  $(E_n < 4.0 \text{ eV})$  are related to the excitation from the ground state to the second excited state  $(S_0 \rightarrow S_2)$ , and the corresponding TPA cross sections are reported in Scheme 1. The  $S_0 \rightarrow S_2$  transition takes place from both HOMO−1 and HOMO to the LUMO and LUMO+1 (Figure 1 and Table S3) and corresponds to a charge transfer from the arylamine edges to the π-deficient heteroaromatics. Although all five b[enzobisthia](#page-3-0)zoles possess stronger electron-accepting ability than the parent benzothiazole, as indicated by NPA charge analysis (Table S4), this feature does not necessarily guarantee a higher NLO response, and no relationship between  $\delta_{\text{TPA}}$  and th[e accepto](#page-3-0)r strength of the  $\pi$ -deficient core can be established. Instead, the



Figure 1. Frontier molecular orbitals in Q2-Ph.

relative position of two thiazole rings on the central benzene plays a key role.

Irrespective of the R substituent, benzobisthiazole dyes are ranked according to increasing TPA cross sections as follows: Q5 < Q4 < Q1 < Q3 < Q2, with a difference of >900 GM between the least and the most efficient TPA dye! The additional thiazole ring has a beneficial effect only in the case of **Q2-Ph**, whereas  $\delta_{TPA}$  of Q2-Me is virtually identical with its benzothiazole analogue. Using a three-state model,<sup>14</sup> the great variation of  $\delta_{\text{TPA}}$  within the isomeric benzobisthiazole series and the strikingly lower TPA cross sections of Q1 [an](#page-3-0)d Q3−Q5 as compared to the benzothiazole congeners can be primarily attributed to the differerent excited-to-excited state transition moments  $\mu_{12}$  and the somewhat larger detuning energies  $(E_1 - E_2/2)$  in the former series (cf. Table S5, Figure S1 in SI for more detailed analysis of the observed trends). In contrast, the superiority of dyes derived from benzobisthiazole 2 over its [iso](#page-3-0)mers is related to a favorable combination of all parameters involved in the three-state model (the highest transition dipole moments  $\mu_{01}$  and  $\mu_{12}$  and the reduced detuning energy). This results from the most efficient coupling between two branches connected to the heteroaromatic ring with two nitrogen and two sulfur atoms in mutual para position, respectively. The lowest  $\mu_{12}$  values are computed for dyes derived from l and 5, where two N and two S atoms, respectively, are in unfavorable meta position. Benzobisthiazoles 3 and 4 are intermediate cases, where one of the N,N or S,S couples is positioned para, while the other one is placed in the ortho position. Substantially higher  $\delta_{\text{TPA}}$  of Q3 over Q4 indicate more important placement of two azole N atoms into a mutual para position, compared to the two sulfur atoms.

To prove these findings, quadrupolar chromophores containing benzobisthiazoles 2 and 3 as the central moiety were prepared and subjected to measurements of  $\delta_{\text{TPA}}$  via a two-photon excited fluorescence (TPEF) method with femtosecond laser excitation at wavelengths of 750−850 nm. The synthesis of other isomers was not attempted due to their anticipated lower TPA activity.

A key step in the synthesis of Q2 and Q3 was a double aldoltype condensation between 4-donor-substituted benzaldehydes and benzobisthiazoles with two active methyl groups (2-Me or 3- Me) under strongly basic conditions (Scheme 2). The starting 2- Me was prepared by a condensation of the commercially available 2,5-diaminobenzene-1,4-dithiol dihydrochlori[de](#page-2-0) (6) with acetic anhydride in the presence of triethylamine as a cosolvent.  $Ac<sub>2</sub>O$ was efficient enough in the one-step formation of a benzobisthiazole scaffold and the use of orthoesters and rareearth metal triflates as catalysts was not necessary, albeit the latter method provides the desired product in somewhat higher yield.<sup>15</sup> **3-Me** was prepared from 6-amino-2-methylbenzothiazole  $(7)^2$ which was first reacted with KSCN and  $Br<sub>2</sub>$  to afford t[he](#page-3-0) thiocyanate 8. This was consequently transformed in one pot t[o](#page-3-0) 3-Me via reduction with  $Na<sub>2</sub>S$  and ring-closing reaction between

<span id="page-2-0"></span>



Figure 2. Intermolecular  $\pi-\pi$  stacking in the unit cell of Q2-Ph·2CHCl<sub>3</sub> (solvent molecules are omitted for clarity, and the displacement ellipsoids are drawn at 50% probability level). The benzobisthiazole molecules are mutually  $\pi$ -stacked with interplanar distance of 3.502(3) Å and slippage of 0.812 Å (see SI for more details).

Table 1. Photophysical [Pro](#page-3-0)perties of Quadrupolar Dyes in Toluene

dye	$\lambda_{\text{abs}}$  nm	$\varepsilon_{\rm max}$ $[M^{-1}cm^{-1}]$	$\Lambda_f$  nm	$\Phi_{\epsilon}$	$\lambda_{\text{TPA}}$  nm	$\delta_{\text{TPA}}\Phi_{\text{f}}$ $\lceil GM \rceil$	$\delta_{\rm TPA}$ $\lceil GM \rceil$
Obtz-Me	417	68500	493	0.17	750	232	1365
<b>Obtz-Ph</b>	431	72400	491	0.56	770	864	1543
$O2-Ph$	445	83900	496	0.94	810	1575	1676
$Q2-Do$	451	85800	499	0.48	810	871	1815
$O3-Me$	440	62300	492	0.20	790	195	975
$Q3-Ph$	442	74600	493	0.50	810	619	1238
$Q3-Do$	448	77200	497	0.31	810	503	1622

 $Ac<sub>2</sub>O$  and the intermediately formed 6-amino-2-methylbenzothiazol-7-thiol.<sup>16</sup>

The presence of a second thiazole ring allows avoiding metalcatalyzed cros[s-c](#page-3-0)oupling reactions to attach the second styryl arm to the central ring, making the synthesis more convenient, cost friendly, and amenable to large-scale production as compared to that of the Qbtz series. Q2-Me was not isolated due to its high insolubility in common organic solvents, presumably due to  $\pi-\pi$ stacking interactions (see Figure 2). No insolubility issue occurred when preparing Q3-Me and all the other derivatives with phenyl (Ph) and dodecyl (Do) substituents at the periphery. All double bonds in the target chromophores formed under the Knoevenagel condensation were trans-configured, as confirmed by the coupling constants of the vinyl protons  $({}^3J_{\rm H,H} \approx 16 \text{ Hz})$  in  ${}^{1}\text{H}$  NMP, spectra and the X-ray structure of **O2-Pb**  $H$  NMR spectra and the X-ray structure of **Q2-Ph**.

The absorption spectra of benzobisthiazole dyes in toluene (Table 1, Figure 3, Figure S5) feature one intense band in the



Figure 3. UV−vis absorption (solid line) and emission (dashed line) spectra of Q2-Ph ( $c = 10 \mu M$ ) in toluene, THF, acetone, and DMSO (left). Fluorescence of Q2-Ph in various organic solvents (right).



Figure 4. TPA action cross sections  $\delta_{\text{TPA}}\cdot\Phi_{\text{f}}$  (left) and TPA cross sections  $\delta_{\text{TPA}}$  (right) of the quadrupolar dyes in toluene.

visible region with maxima  $\lambda_{\text{abs}}$  in the range of 440–451 nm (11– 23 nm bathochromically shifted compared to the Qbtz series), with one shoulder peak on the low-energy side. This multicomponent pattern is also seen in emission spectra (Figure S5) and can be related to the vibronic coupling. The fluorescence in toluene is observed in the blue-green spectral region with [the](#page-3-0) most intense peaks at 490−500 nm. While  $\lambda_{\text{abs}}$  remains essentially unchanged upon increasing solvent polarity, a pronounced red shift is observed for fluorescence maxima  $\lambda_f$  (Figure 3).

TPEF spectra of the prepared dyes are in toluene shown in Figure 4. All benzobisthiazole chromophores exhibit moderate to excellent TPA cross sections (975–1815 GM), with maxima  $\lambda_{\text{TPA}}$ positioned at 790−810 nm (Table 1). This is substantially less than twice that of the single-photon absorption  $\lambda_{\text{abs}}$  (S<sub>0</sub>  $\rightarrow$  S<sub>1</sub>), implying a  $S_0 \rightarrow S_2$  transition as expected for quadrupolar dyes due to parity selection rules.  $\lambda_{\text{TPA}}$  of Qbtz-Me and Qbtz-Ph are blue-shifted to 750 and 770 nm, respectively, consistent with the somewhat higher second excitation energies  $E_2$  calculated for these derivatives. The highest  $\delta_{\text{TPA}}$  (>1600 GM) are observed for Q2-Do, Q2-Ph, and Q3-Do.

The efficiency of central heteroaromatic rings is assessed by comparing  $\delta_{TPA}$  of triphenylamine end-capped derivatives, establishing the following order: Q3-Ph < Qbtz-Ph < Q2-Ph. This is in agreement with our computations and confirms (a) a slight superiority of the linear centrosymmetric benzobisthiazole 2 over benzothiazole and (b) lower TPA activity of dyes derived from angular benzobisthiazole 3 compared with its linear congener 2 and benzothiazole analogue (this is also evident from comparing Q3-Do to Q2-Do and Q3-Me to Qbtz-Me). Although the difference between  $\delta_{TPA}$  of **Q2-Ph** and **Qbtz-Ph** is rather small, the former exhibits a fluorescent quantum yield more than twice as large, resulting in substantially higher TPA action cross section,  $\delta_{\text{TPA}}\Phi_f$  (Figure 4, left). Since the latter quantity is vital in TPEF microscopy, where both strong TPA and one-photon emission are required, Q2-Ph is an excellent candidate for two-photon imaging.

<span id="page-3-0"></span>Similar to our previous findings, derivatives decorated with a diphenylamino group exhibit larger NLO response than their dimethylamino analogues (Qbtz-Me vs Qbtz-Ph, Q3-Me vs Q3- Ph). TPA enhancement is even more pronounced when employing a didodecylamino group (Q2-Ph vs Q2-Do, Q3-Ph vs Q3-Do). This somewhat counterintuitive behavior is confirmed by our calculations $17$  and can be rationalized by involving additional optical channels in triphenylamine series, which to some extent reduce the  $\delta_{\text{TPA}}$  values obtained from the three-state model (cf. Table S6). Both the elongation of pendant alkyl chains and the extension of  $\pi$ -conjugation using a diarylamino moiety offer thus a useful strategy not only to increase the solubility but also to amplify  $\delta_{\text{TPA}}$ , where the latter modification is revealed as more suitable for engineering highly emissive fluorophores.

To conclude, the fusion of the additional  $\pi$ -deficient heteroaromatic ring to the central electron-accepting core must not necessarily lead to TPA enhancement, as intuitively expected, and may even have a detrimental effect on the NLO response (Qbtz vs Q1, Q3−Q5). To benefit from this structural modification, the relative position of heteroaromatic moieties attached to the central ring has to be optimized to ensure an efficient electronic coupling, which results in favorable onephoton absorption parameters and an enhanced TPA response. In this respect, the Q2 series with excellent TPA cross sections  $(\delta_{TPA} > 1600 \text{ GM})$ , high emission quantum yields, and a facile method for synthesis provides a low-cost and very efficient alternative to many TPA fluorophores currently used.<sup>18</sup> In addition, all benzobisthiazoles have further possible points of attachment, allowing for more modifications to modulate and improve TPA cross sections using the same building block, for example, by introducing auxiliary electron donor or acceptor substituents on the heteroaromatic ring or by building multibranched structures via coordination of heterocyclic nitrogen atoms to metal ions.

# **ASSOCIATED CONTENT**

### **S** Supporting Information

Experimental and computational details, computed TPA cross sections and one-photon absorption characteristics, detailed quantum-chemical analysis, synthetic procedures, and crystal structure data for  $Q2-Ph \cdot 2CHCl_3$ . This material is available free of charge via the Internet at http://pubs.acs.org.

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### **Notes**

The authors declare no competing financial interest.

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(17) See Figure S2 for a dependence of  $\delta_{\rm TPA}$  on the pendant alkyl chain length in Q2-R series, where  $\delta_{\rm TPA}$  increases steadily to reach a plateau for the dioctylamino group. Despite the higher  $\mu_{01}$  and  $\mu_{12}$  values for the  $NPh<sub>2</sub>$  end-capped derivative, its TPA activity is comparable to that of the NHex<sub>2</sub> analogue.

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